

Warm-up

Work on your Warm-up.



1. What is the difference between expression and equation?

$$x^2 \cdot x^2 = x^4$$

$$\sqrt{\frac{1}{4}} = \frac{\sqrt{1}}{\sqrt{4}} = \frac{1}{2}$$

Simplify the following expressions:

$$x^4 - 9$$

$$(x^2 - 3)(x^2 + 3)$$

$$\frac{1}{4}x^2 - 36$$

$$\left(\frac{1}{2}x - 6\right)\left(\frac{1}{2}x + 6\right)$$

$$x^2 + 49$$

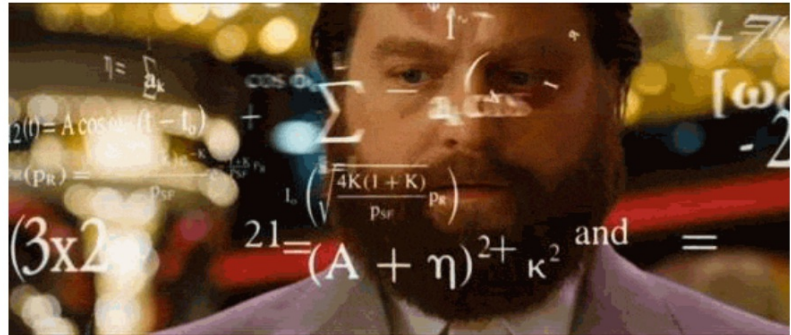
not factorable

Agenda:

1) Completing the square to solve quadratic equations! - Notes

2) Bingo

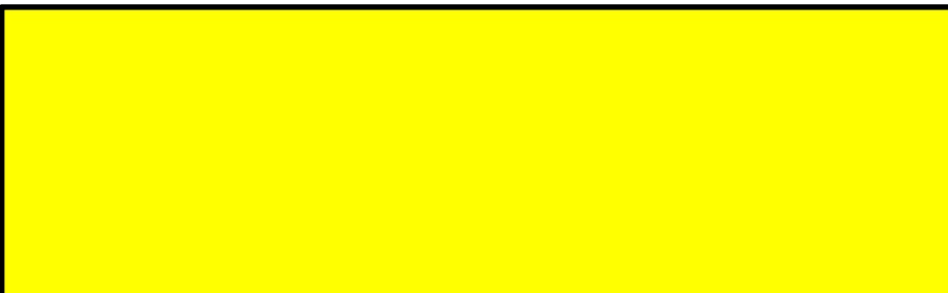
3) Exit Ticket



Few terms to consider...

Since now we are *solving* quadratic equations now... 

- We are going to get solutions.
- Other words for "solutions":
 - "Roots"
 - "Zeros"



Steps for Completing the Square

Key Concepts, *continued*

Completing the Square to Solve Quadratics

1. Make sure the equation is in standard form, $ax^2 + bx + c$. [REDACTED]
2. Subtract c from both sides.
3. Divide each term by a to get a leading coefficient of 1. [REDACTED]
4. Add the square of half of the coefficient of the x -term to both sides to complete the square. [REDACTED]
5. Express the perfect square trinomial as the square of a binomial. ★★ ★★ ★★
6. Solve by using square roots.

$$\left(\frac{b}{2}\right)^2$$



$$x^2 + 2x - 15 = 0$$

$$+15 \quad +15$$

$$x^2 + 2x = 15$$

$$x^2 + 2x + 1 = 15 + 1$$

$$\sqrt{(x+1)^2} = \sqrt{16}$$

$$x+1 = \pm 4$$

$$\begin{array}{r} -1 \\ -1 \end{array}$$

$$\frac{2}{2} = 1^2 = 1$$

$x = 3, -5$

Solve by completing the square: $\frac{5}{2} = \left(\frac{5}{2}\right)^2$

$$3x^2 + 15x + 12 = 0$$

$$-12 \quad -12$$

$$\frac{3x^2 + 15x}{3} = \frac{-12}{3}$$

$$x^2 + 5x = -4$$

$$x^2 + 5x + \frac{25}{4} = -4 + \frac{25}{4}$$

$$\sqrt{\left(x + \frac{5}{2}\right)^2} = \sqrt{\frac{9}{4}}$$

$$x + \frac{5}{2} = \pm \frac{3}{2}$$

$$\begin{array}{r} -\frac{5}{2} \\ -\frac{5}{2} \end{array}$$

$x = -1, -4$

$$2x^2 + 8x - 7 = -2$$

$$+7 \quad +7$$

$$\frac{2x^2 + 8x}{2} = \frac{5}{2}$$

$$x^2 + 4x = \frac{5}{2}$$

$$x^2 + 4x + 4 = \frac{5}{2} + 4$$

$$\sqrt{(x+2)^2} = \sqrt{\frac{13}{2}}$$

$$x+2 = \pm \sqrt{\frac{13}{2}}$$

$$\begin{array}{r} -2 \\ -2 \end{array}$$

$$\frac{4}{2} = 2^2 = 4$$

$x = -2 \pm \sqrt{\frac{13}{2}}$

In your own words, what is the most confusing step for you?

Solve by completing the square:

$$6x^2 + 18x + 12 = 0$$

$$\frac{3}{2} = \left(\frac{3}{2}\right)^2 = \frac{9}{4}$$

$$\frac{6x^2}{6} + \frac{18x}{6} = \frac{-12}{6}$$

$$\sqrt{\left(x + \frac{3}{2}\right)^2} = \sqrt{\frac{1}{4}}$$

$$x^2 + 3x = -2$$

$$x + \frac{3}{2} = \pm \frac{1}{2}$$

$$x^2 + 3x + \frac{9}{4} = -2 + \frac{9}{4}$$

$$-\frac{3}{2} \quad -\frac{3}{2}$$

$$2x^2 - 4x + 5 = 6$$

$$\frac{-2}{2} = -1^2 = 1$$

$$x = \frac{1}{2} - \frac{3}{2} = \frac{-2}{2} = -1$$
$$x = -\frac{1}{2} - \frac{3}{2} = \frac{-4}{2} = -2$$

$$\frac{2x^2}{2} - \frac{4x}{2} = \frac{1}{2}$$

$$x^2 - 2x = \frac{1}{2}$$

$$x^2 - 2x + 1 = \frac{1}{2} + 1$$

$$\sqrt{(x-1)^2} = \sqrt{\frac{3}{2}}$$

$$x-1 = \pm \sqrt{\frac{3}{2}}$$

$$x = 1 \pm \sqrt{\frac{3}{2}}$$

$$\text{II) } k^2 - 4k + 1 = -5$$

$$\frac{-4}{2} = -2^2 = 4$$

$$k^2 - 4k = -6$$

$$k^2 - 4k + \underline{4} = -6 + \underline{4}$$

$$\sqrt{(k-2)^2} = \sqrt{-2}$$

$$k-2 = \pm\sqrt{-2}$$

$$k-2 = \pm i\sqrt{2}$$

$$+2 \quad +2$$

$$k = 2 \pm i\sqrt{2}$$